## **SSP Exercise 7 Solutions**

1. Add impurity atoms with +1 valence relative to host semiconductor; excess electron is ionised by thermal energy and electron donated to conduction band. Add impurity atoms with -1 valence relative to host semiconductor; excess hole ionised by thermal energy and accepted by valence band. [5]

2. (i) 
$$n_{\rm D}^+ = N_{\rm D} \left[ \frac{1}{\exp((\varepsilon_{\rm D} - \varepsilon_{\rm F}) / k_{\rm B}T) + 1} \right]$$

In the freeze-out region the conduction band electron density will be equal to  $n_{\rm D}^+$ , and exp(( $\epsilon_{\rm D} - \epsilon_{\rm F}$ )/ $k_{\rm B}T$ )>>1, therefore the low temperature region of the right-hand graph will be of gradient (( $\epsilon_{\rm D} - \epsilon_{\rm F}$ )/ $k_{\rm B}$ ).



The measured gradient is ~ 245

$$\Rightarrow (\varepsilon_{\rm D} - \varepsilon_{\rm F}) \approx 20 \text{ meV} \qquad [4]$$

(ii) and (iii)  $n_{\rm i} = W^{\frac{1}{2}} T^{\frac{3}{2}} e^{-\frac{\varepsilon_{\rm g}}{2k_{\rm B}T}}$ , therefore the gradient of the left-hand graph will be *approximately* (- $\varepsilon_{\rm g}/2k_{\rm B}$ )



For GaAs, the measured gradient is 
$$\sim 9800$$

$$\Rightarrow \epsilon_{\rm g} \approx 1.7 \text{ eV}$$
[3]